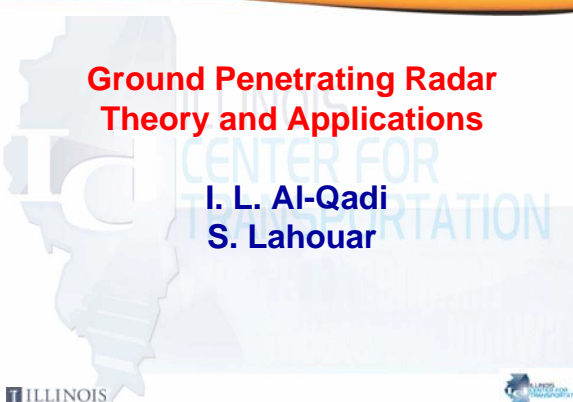



Ground Penetrating Radar Theory and Applications

I. L. Al-Qadi
S. Lahouar




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Presentation Overview

- Background
 - Nondestructive Testing
 - GPR Systems
 - Electromagnetic Theory
 - GPR Data Analysis
- GPR Applications
 - Flexible Pavements
 - Rigid Pavements
 - Rail Road




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Introduction

- US transportation infrastructure is deteriorating:
 - 2005 ASCE Report card for American Transportation Infrastructure gave an overall grade of “D” – estimated \$1.3 trillion investment needed for improvements
- Transportation agencies are shifting efforts from building new to assessing and rehabilitating existing structures

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What is NDE?



Non-destructive evaluation

Detect defects, internal distresses, measure dimensions, etc. w/o damaging the material

- Ultrasonic waves
- X-ray/ CAT scans
- RADAR scanning
- Thermal imaging
- etc

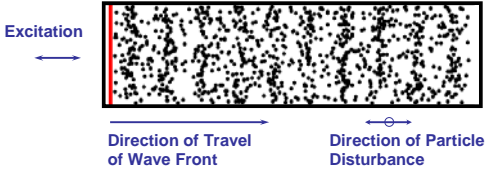


X-ray radiograph

What Are Waves?



Propagation of a disturbance through a medium
(mass is not transported in propagation direction)



Excitation ←

→ Direction of Travel of Wave Front ← Direction of Particle Disturbance

Important parameters:
wavelength (λ), period (T) and frequency (f)

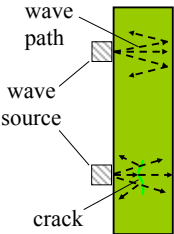
Ultrasonic Testing (UT)

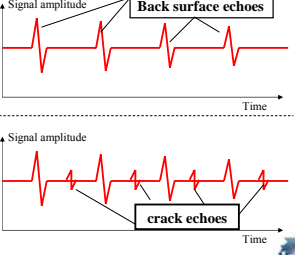
Flaw detection: wave echoes from air-filled defects such as cracks and voids



wave path

wave source

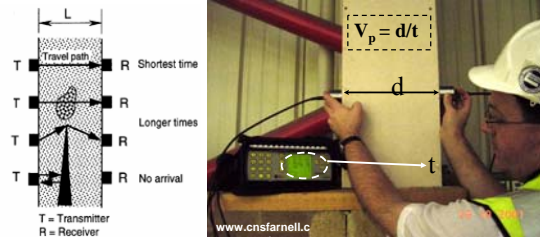
crack





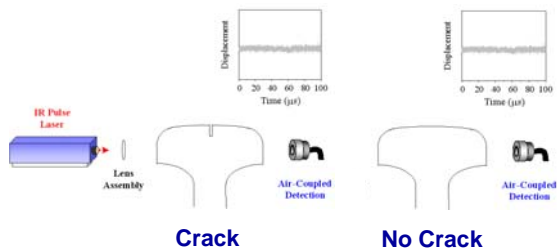
Ultrasonic Pulse Velocity (UPV)



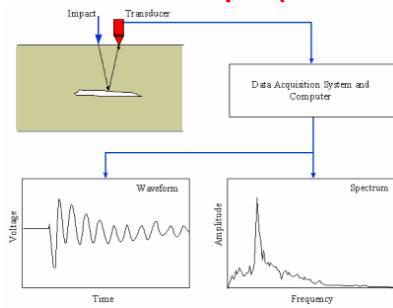
v_p related to in-place material strength or presence of internal voiding and cracking (Frequency 20-200MHz)



Approach Illustration



Impact Echo Principle (ASTM C1383)



Reflected waves set up a resonance condition having a characteristic frequency (like a bell)



Concrete Element Inspection

2- and 3-D maps of backscatter intensity (courtesy of BAM)

GPR Applications

- Ground Penetrating Radar (GPR): special kind of RADAR
- GPR usage:
 1. Detect buried targets
 2. Estimate their depths
- GPR applications:
 - Geophysics: estimate structure of earth sediments
 - Archeology: locate buried archeological structures
 - Safety tool: locate landmines
 - **Civil Engineering: evaluate performance of civil structures (buildings, bridges, pavements...)**

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GPR History

- Early 1900's: RADAR Principle Was Used to Detect Airborne Objects
- Hulsenberg (1926): Detection of Buried Objects
- Austria (1929): Depth of Glacier
- Late 1950's: US Air force plane crashed in Greenland because of wrong altitude from Radar

⇒ Ability of Radar to See Into Subsurface

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GPR History

- 1960's: Moon Surface Characterization by NASA
 - Ground Probing Radar Systems Were Used in Geological Applications
- Vietnam War: "Combat Radar" Was Used to Locate Mines, Tunnels, and Bunkers
- 1970's: Locating Sewer Lines and Cables, Measuring Ice Thickness, Profiling Bottom of Lakes and Rivers
- 1980's-now: Different Applications Related to Pavements and Bridge Decks

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EM Properties of Materials

Interaction of a Material with Applied Electric (E) and Magnetic (H) Fields:

- Polarization
- Conductivity
- Magnetic Permeability
- **Permittivity/ Dielectric Constant**

$$\epsilon_r = \epsilon_r' - j\epsilon_r''$$

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Polarization

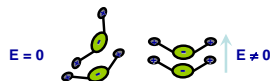
• **Electronic Polarization:**



• **Ionic Polarization:**



• **Molecular Polarization:**



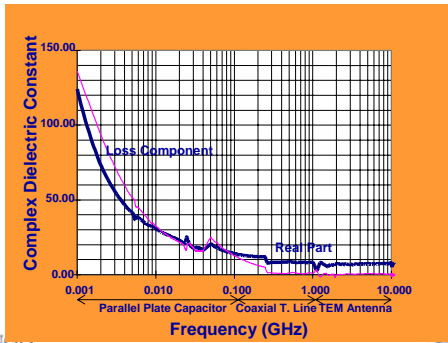
• **Interfacial Polarization:**



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DIELECTRIC PROPERTIES OF CONCRETE



Typical Dielectric Constant Values

Material	Dielectric Constant
Air	1
Water	81
Concrete	3-18
HMA	3-10
Limestone	5-9
Granite	4-6
Dry Sand	3-5
Saturated Sand	20-30
Silts	5-30
Clays	5-40

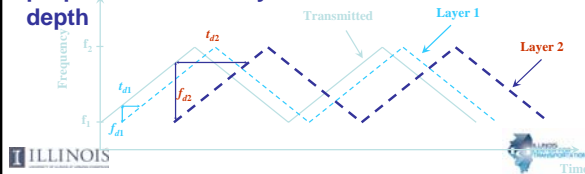
GPR Types

Three main types of GPR systems:

- Frequency modulated GPR
- Synthetic pulse GPR
- Pulsed (or impulse) GPR

Frequency Modulated GPR

- Change frequency of transmitted signal linearly between two limits
- Frequency difference (transmitted - reflected) proportional to the layer depth



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Time

Synthetic Pulse GPR

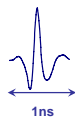
- Change frequency of transmitted signal between two limits in discrete steps
- Amplitude and phase of reflected signal at each frequency step are recorded
- Reflected signal reconstructed in the time domain using an IFFT algorithm

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Pulsed or Impulse GPR

- Most common type of GPR systems
- Transmitted signal is a short pulse (1 ns or less)
- Principle: Transmit a short pulse and record the reflected pulses from layer interfaces



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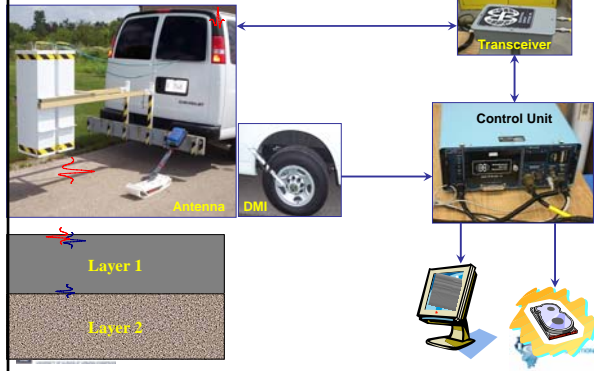
GPR Antennas

- Ground-coupled: the antenna is in contact with the ground surface
- Air-coupled: the antenna is 0.5m above surface
- Monostatic: one antenna used as Tx and Rx
- Bistatic: one antenna is used for Tx and another one for Rx



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GPR: How does it work?



Reflection & Transmission

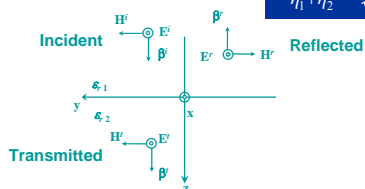
At normal incidence:

- Reflection coefficient:

$$\gamma = \frac{\eta_2 - \eta_1}{\eta_2 + \eta_1} = \frac{\sqrt{\epsilon_{r1}} - \sqrt{\epsilon_{r2}}}{\sqrt{\epsilon_{r1}} + \sqrt{\epsilon_{r2}}}$$

- Transmission coefficient:

$$\tau = \frac{2\eta_2}{\eta_1 + \eta_2} = \frac{2\sqrt{\epsilon_{r1}}}{\sqrt{\epsilon_{r1}} + \sqrt{\epsilon_{r2}}}$$



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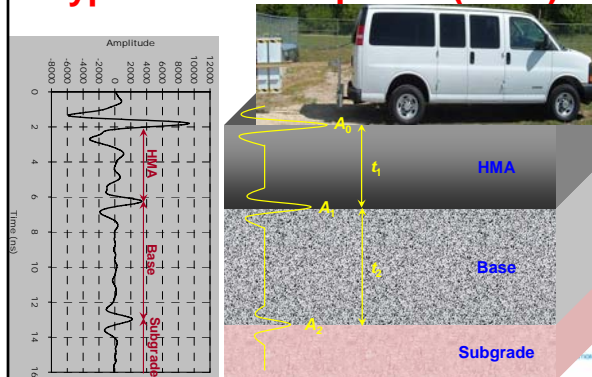
EM Scattering

- EM scattering: occurs when there is a *discontinuity* in the dielectric properties of a medium
- For pavements a discontinuity can be:
 - Layer interface
 - Distress within the layer
- At a discontinuity:
 - Reflection
 - Transmission

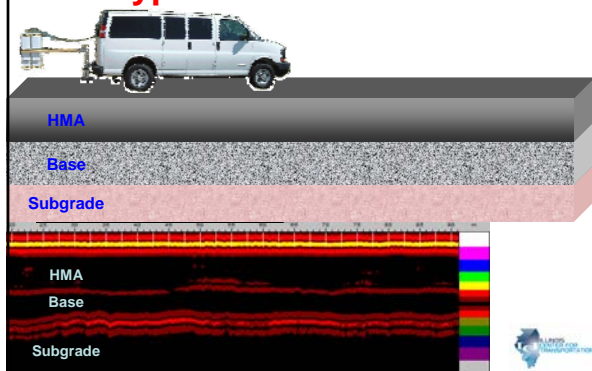
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Typical GPR Response (scan)



Typical Raw GPR Data



GPR Applications

- **Layer thickness estimation**
 - QC/QA: new pavements
 - Structure evaluation: in service pavements
- **Subsurface Moisture/ Distress detection**
- **Rebar/ Dowel Localization**
- **Rebar Cover Depth Estimation**
- **Railroad Evaluation (Ballast)**

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Typical Problems with GPR Data Interpretation

- GPR doesn't provide "real" images of the subsurface
- Dielectric properties unknown
 - Dielectric properties change with depth (especially in the presence of moisture)
- Thin pavement layers are difficult to resolve
- Extensive amount of data
- GPR results are operator dependent

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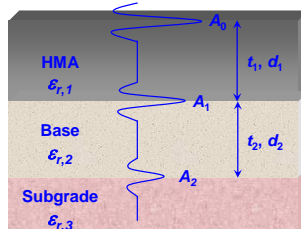
Layer Thickness Estimation

Thickness of i^{th} layer:

$$d_i = \frac{ct_i}{2\sqrt{\epsilon_{r,i}}}$$

where: $\epsilon_{r,i} = \left(\frac{A_p - A_o}{A_p + A_o} \right)^2$,

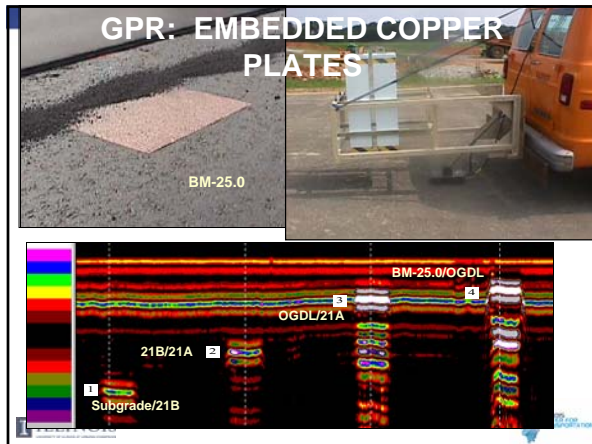
$$\epsilon_{r,p} = \epsilon_{r,p+1} \left(\frac{1 - \left(\frac{A_0}{A_p} \right)^2 + \sum_{i=1}^{p-2} \gamma_i \frac{A_i}{A_p} + \frac{A_{p-1}}{A_p}}{1 - \left(\frac{A_0}{A_p} \right)^2 + \sum_{i=1}^{p-2} \gamma_i \frac{A_i}{A_p} - \frac{A_{p-1}}{A_p}} \right)^2$$

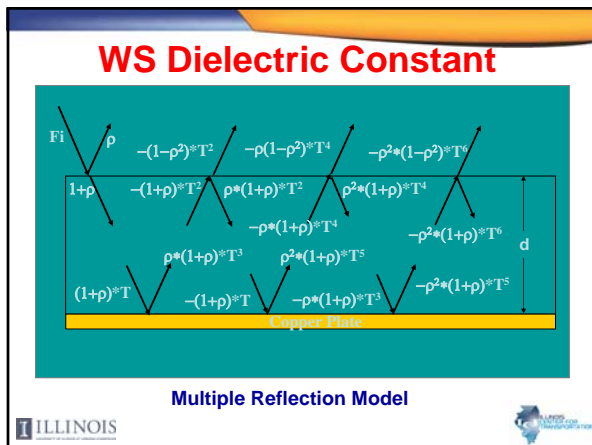


$$\gamma_i = \frac{\sqrt{\epsilon_{r,i}} - \sqrt{\epsilon_{r,i+1}}}{\sqrt{\epsilon_{r,i}} + \sqrt{\epsilon_{r,i+1}}}$$

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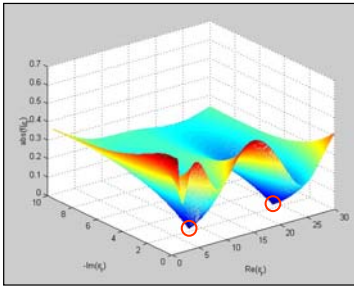
Input Reflection Coefficient

$$\Gamma = \frac{FT(Y_r)}{FT(Y_i)} = \frac{F_r}{F_i} = \rho - T^2 (1 - \rho^2) \frac{1 - (\rho T^2)^{n+1}}{1 - \rho T^2} = \rho - T^2 (1 - \rho^2) \sum_{i=1}^n (\rho T^2)^i$$

with: $\rho = \frac{1 - \sqrt{\epsilon_r^*}}{1 + \sqrt{\epsilon_r^*}}$ and $T = e^{-j\frac{\omega}{c}\sqrt{\epsilon_r^*}d} = e^{-j\frac{\omega}{c}\frac{1-p}{1+p}d}$

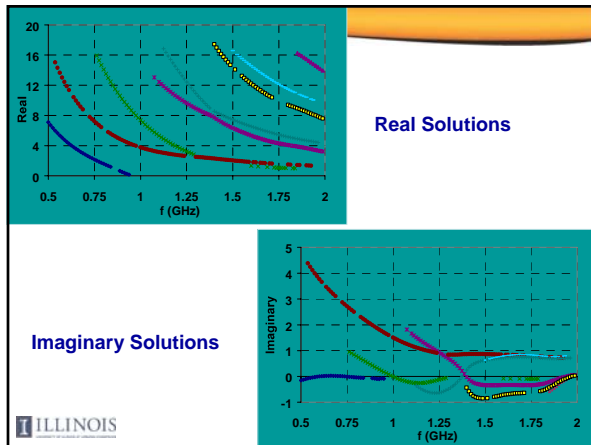
To find ϵ_r , Solve: $f(\rho) = \rho - T^2 (1 - \rho^2) \frac{1 - (\rho T^2)^{n+1}}{1 - \rho T^2} - \frac{F_r}{F_i} = 0$

Multiple Solutions



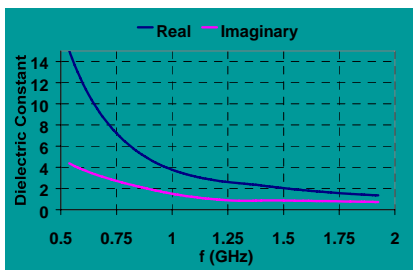
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Physical Solution



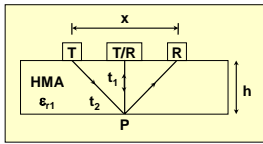
Dielectric Constant for SM-12.5D

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Thickness Estimation Using CMP Technique (more accurate)

Common midpoint (CMP) technique (or common-depth point, CDP) is used as follows:



v : EM velocity in the layer

$$vt_1 = 2h \Rightarrow$$

$$vt_2 = 2\sqrt{h^2 + \left(\frac{x}{2}\right)^2}$$

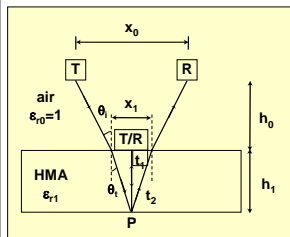
$$v = \frac{c}{\sqrt{\epsilon_r}} = \frac{x}{\sqrt{t_2^2 - t_1^2}}$$

$$\epsilon_r = \frac{c^2(t_2^2 - t_1^2)}{x^2}$$

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Thickness Estimation Using Modified CMP Technique



Snell's law of refraction:

$$\sqrt{\epsilon_{r0}} \sin \theta_i = \sqrt{\epsilon_{r1}} \sin \theta_t \quad (1)$$

Using the figure:

$$2h_0 \tan \theta_i + x_1 = x_0 \quad (2)$$

$$\tan \theta_t = \frac{x_1}{2h_1} = \frac{x_1}{vt_1} \quad (3)$$

$$v = \frac{x_1}{\sqrt{t_2^2 - t_1^2}} \quad (4)$$

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Thickness Estimation Using Modified CMP Technique

Algorithm:

1. Measure the reflection times t_1 and t_2
2. Calculate the transmission angle θ_t using: $\tan \theta_t = \frac{\sqrt{t_2^2 - t_1^2}}{t_1}$
3. Find the angle θ_i by solving numerically

$$2h_0 \tan \theta_i + c \frac{\sin \theta_t}{\sin \theta_i} \sqrt{t_2^2 - t_1^2} = x_0$$

4. Solve for ϵ_{r1} using: $\epsilon_{r1} = \left(\frac{\sin \theta_t}{\sin \theta_i}\right)^2$

5. Compute HMA thickness using

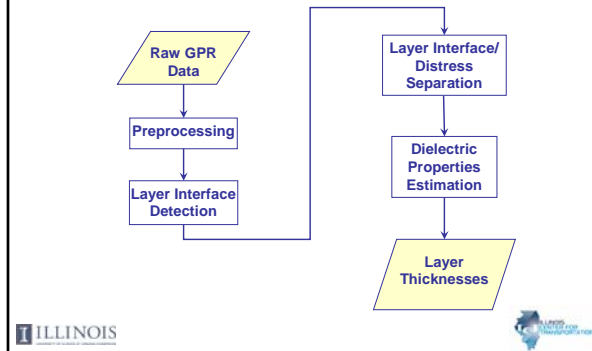
$$t_1 \text{ and } \epsilon_{r1} \quad h_1 = ct_1 / 2\sqrt{\epsilon_{r1}}$$

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Modified CMP Setup

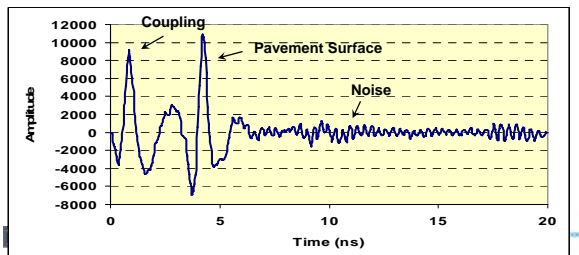
Automated GPR Data Analysis



Preprocessing

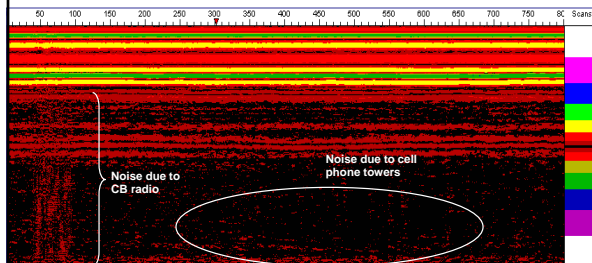
Enhance signal quality:

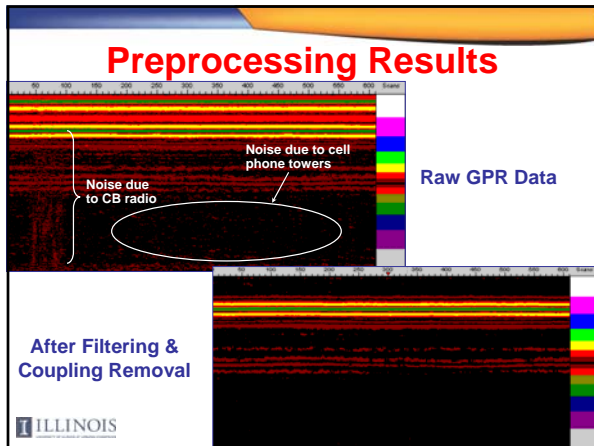
- Noise filtering
- Coupling pulse removal

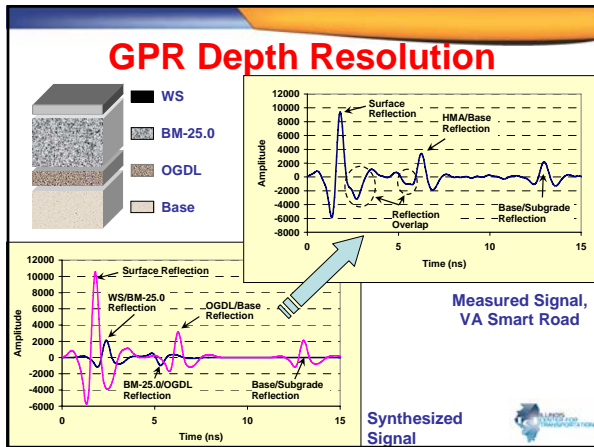


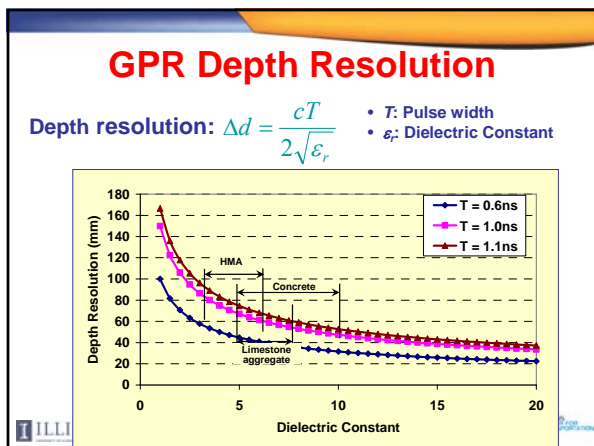
Noise Filtering

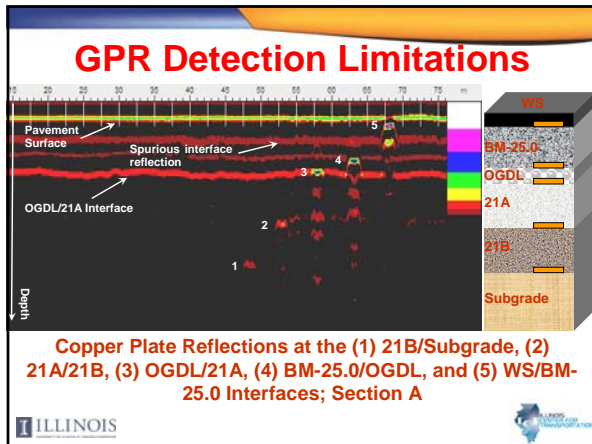
- GPR susceptible to EM noise: CB radios, cell phones, cell phone towers, etc.











- ### Depth Resolution Enhancement
- Inverse filtering
 - Predictive deconvolution
 - Pulse spiking
 - Pulse shaping
 - Homomorphic deconvolution
- } Wiener Filter
- ILLINOIS

Inverse Filtering

- Implemented as a Wiener filter
- Desired output: impulse at time $t=0 \Rightarrow \delta(t)$
- Incident signal assumed unknown
- Filter designed according to:

$$\begin{bmatrix} r_{yy}(0) & r_{yy}(1) & r_{yy}(2) & \dots & r_{yy}(N-1) \\ r_{yy}(1) & r_{yy}(0) & r_{yy}(1) & \dots & r_{yy}(N-2) \\ r_{yy}(2) & & r_{yy}(0) & & r_{yy}(N-3) \\ \vdots & & & \ddots & \vdots \\ r_{yy}(N-1) & \dots & \dots & \dots & r_{yy}(0) \end{bmatrix} \begin{bmatrix} a_0 \\ a_1 \\ a_2 \\ \vdots \\ a_{N-1} \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}$$

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Predictive Deconvolution

- Implemented as a Wiener filter
- Desired output: reflected signal advanced by α samples $\Rightarrow y(t + \alpha)$
- Incident signal assumed unknown
- Filter designed according to:

$$\begin{bmatrix} r_{yy}(0) & r_{yy}(1) & r_{yy}(2) & \cdots & r_{yy}(N-1) \\ r_{yy}(1) & r_{yy}(0) & r_{yy}(1) & \cdots & r_{yy}(N-2) \\ r_{yy}(2) & r_{yy}(1) & r_{yy}(0) & \cdots & r_{yy}(N-3) \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ r_{yy}(N-1) & \cdots & \cdots & \cdots & r_{yy}(0) \end{bmatrix} \begin{bmatrix} a_0 \\ a_1 \\ a_2 \\ \vdots \\ a_{N-1} \end{bmatrix} = \begin{bmatrix} r_{yy}(\alpha) \\ r_{yy}(\alpha+1) \\ r_{yy}(\alpha+2) \\ \vdots \\ r_{yy}(\alpha+N-1) \end{bmatrix}$$

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Pulse Spiking

- Implemented as a Wiener filter
- Desired output: an impulse (or spike) at a lag l
- Incident signal should be known
- Filter designed according to:

$$\begin{bmatrix} r_{xx}(0) & r_{xx}(1) & r_{xx}(2) & \cdots & r_{xx}(N-1) \\ r_{xx}(1) & r_{xx}(0) & r_{xx}(1) & \cdots & r_{xx}(N-2) \\ r_{xx}(2) & r_{xx}(1) & r_{xx}(0) & \cdots & r_{xx}(N-3) \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ r_{xx}(N-1) & \cdots & \cdots & \cdots & r_{xx}(0) \end{bmatrix} \begin{bmatrix} a_0 \\ a_1 \\ a_2 \\ \vdots \\ a_{N-1} \end{bmatrix} = \begin{bmatrix} x(l) \\ x(l-1) \\ \vdots \\ x(0) \\ 0 \\ \vdots \\ 0 \end{bmatrix}$$

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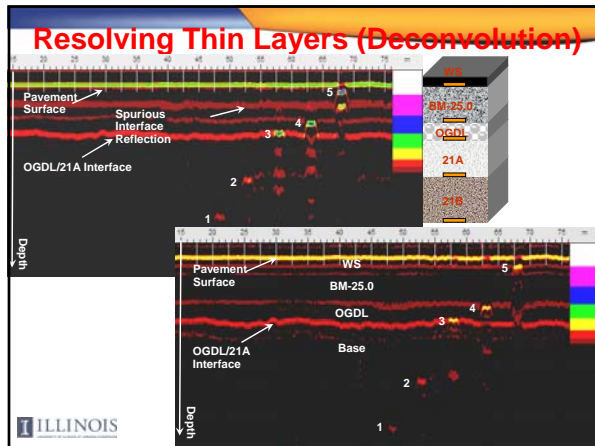
Pulse Shaping

- Implemented as a Wiener filter
- Desired output: a pulse with a fixed shape $s(t)$ at a given lag l
- Incident signal should be known
- Filter designed according to:

$$\begin{bmatrix} r_{xx}(0) & r_{xx}(1) & r_{xx}(2) & \cdots & r_{xx}(N-1) \\ r_{xx}(1) & r_{xx}(0) & r_{xx}(1) & \cdots & r_{xx}(N-2) \\ r_{xx}(2) & r_{xx}(1) & r_{xx}(0) & \cdots & r_{xx}(N-3) \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ r_{xx}(N-1) & \cdots & \cdots & \cdots & r_{xx}(0) \end{bmatrix} \begin{bmatrix} a_0 \\ a_1 \\ a_2 \\ \vdots \\ a_{N-1} \end{bmatrix} = \begin{bmatrix} r_{xx}(l) \\ r_{xx}(l+1) \\ r_{xx}(l+2) \\ \vdots \\ r_{xx}(l+N-1) \end{bmatrix}$$

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Layer Interface Detection

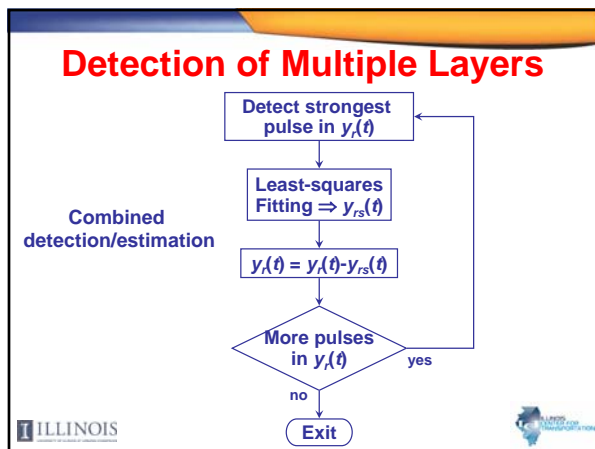
- Purpose:
- Detect layer interface reflections
- Estimate layer interface reflection time-delays

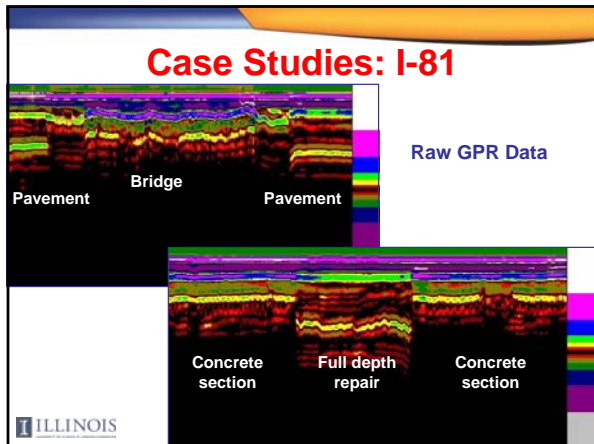
TD reflected signal:

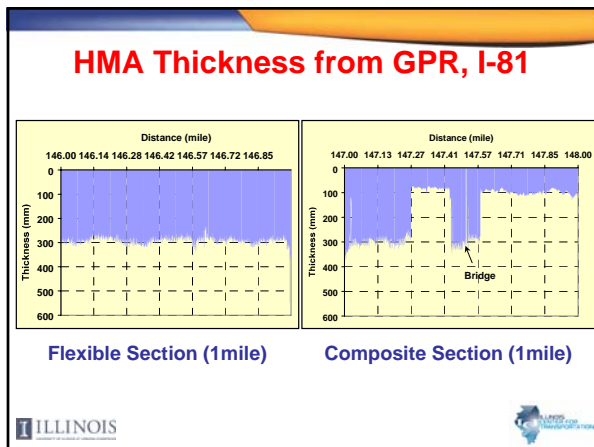
$$y_r(t) = \sum_{i=0}^{N-1} A_i x(t - \sum_{j=0}^i t_j) + n(t)$$

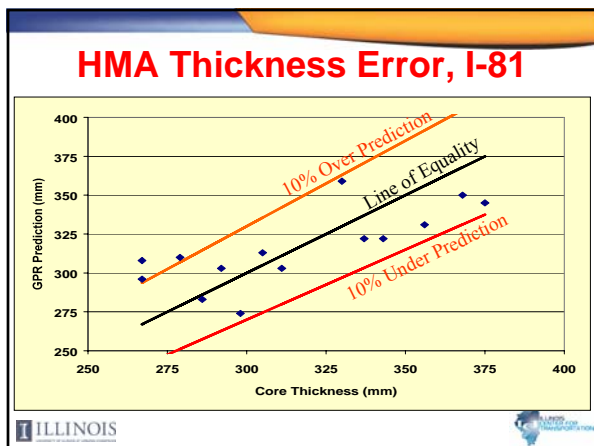
$x(t)$: Incident signal
 $n(t)$: Additive noise

The graph shows the TD reflected signal with Amplitude on the y-axis (ranging from -8000 to 12000) and Time (ns) on the x-axis (ranging from 0 to 15). The signal shows multiple peaks corresponding to layer interfaces.

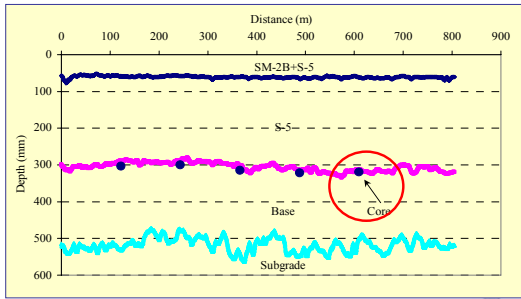








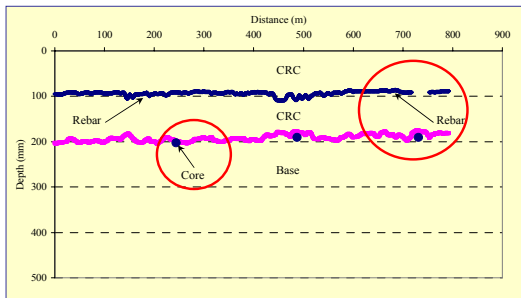
GPR Results: 18 Prem. Sites (Flexible)



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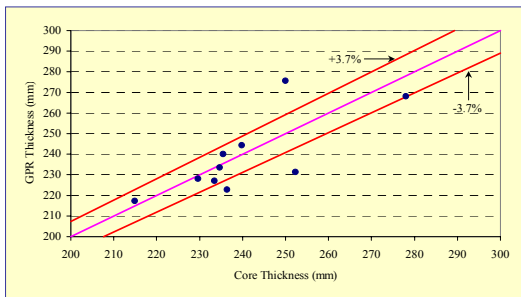
GPR Results: 18 Prem. Sites (Rigid)



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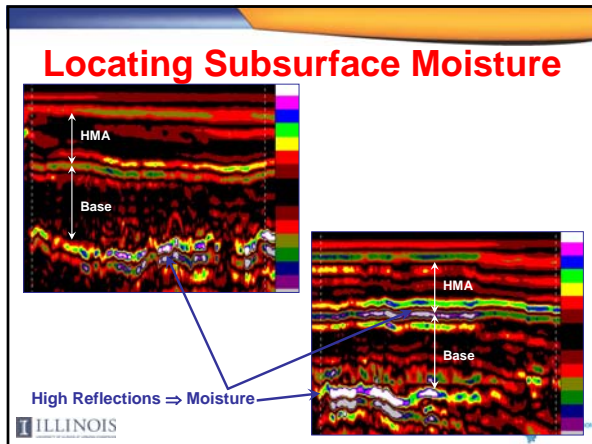


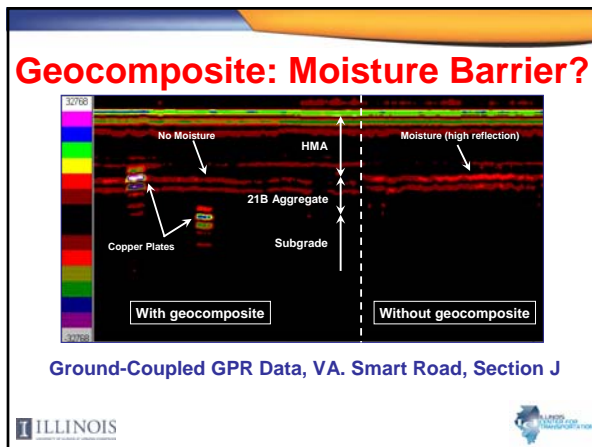
GPR Accuracy (18 Prem. Sites)

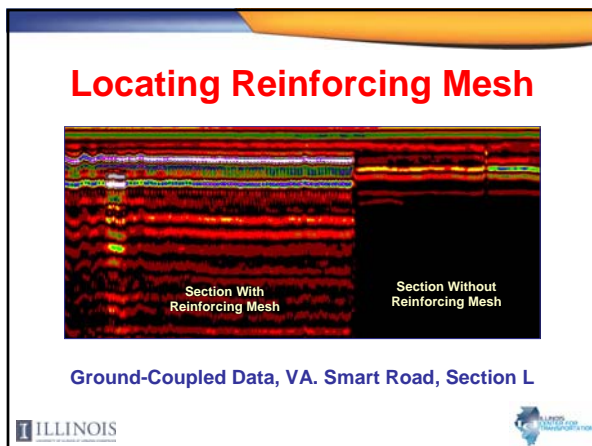


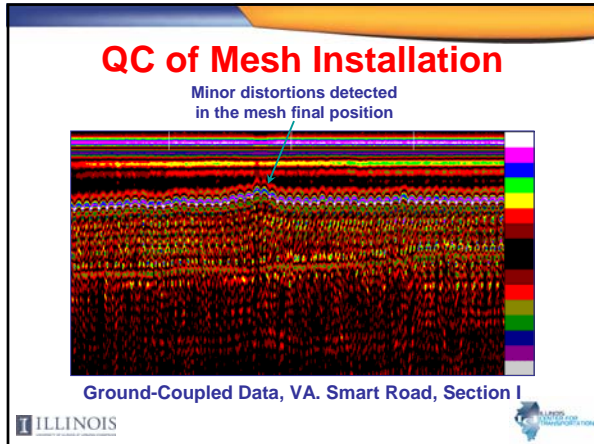
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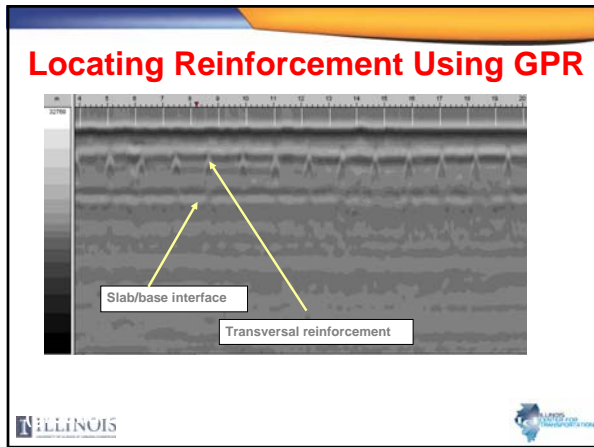


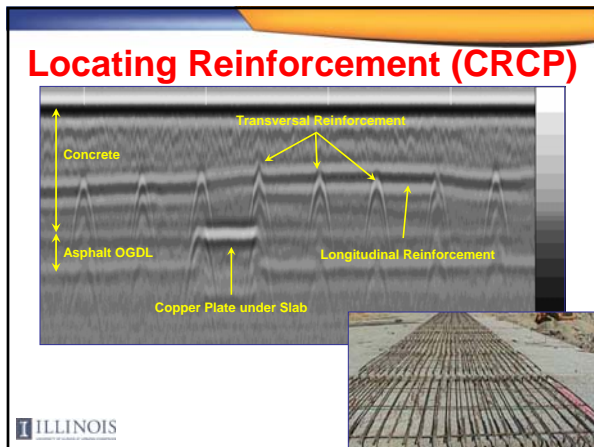


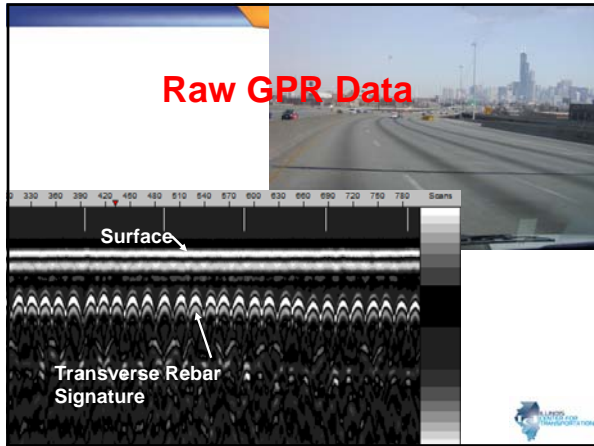


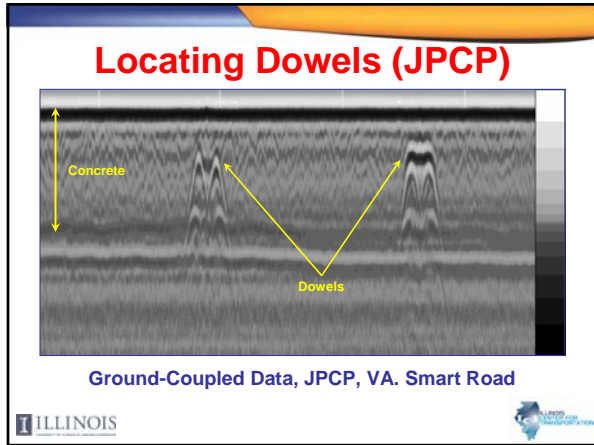


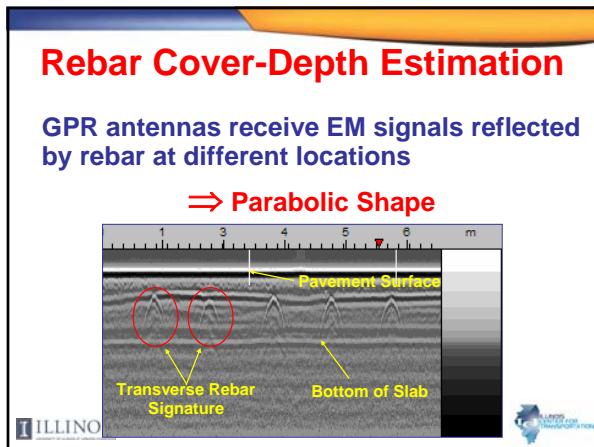


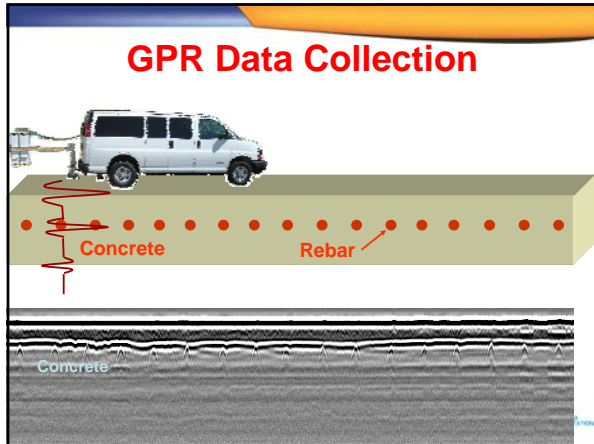


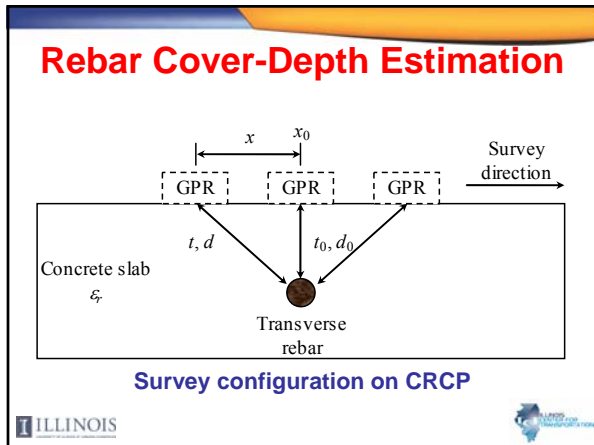












Rebar Cover-Depth Estimation

From the previous configuration we have:

$$t^2 = \frac{4}{v^2} x^2 - \frac{8x_0}{v^2} x + t_0^2 + \frac{4x_0^2}{v^2}$$

with: $v = \frac{c}{\sqrt{\epsilon_r}}$

Rebar Cover-Depth Estimation Algorithm

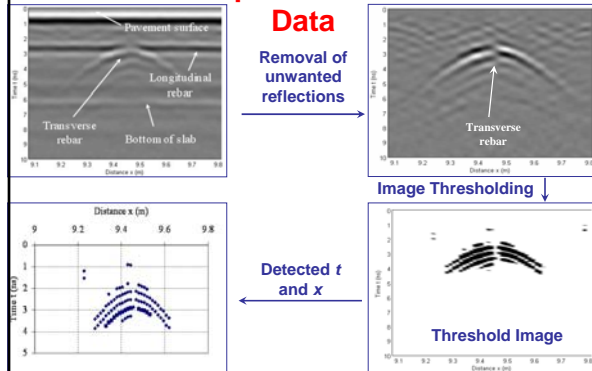
- Measure the time t and the distance x from GPR data (using image processing techniques)
- Estimate the parameters v , t_0 , and x_0 by nonlinearly fitting t and x to the model
- Estimate the dielectric constant ϵ_r
- Estimate the rebar cover-depth d_0 :

$$d_0 = \frac{vt_0}{2}$$

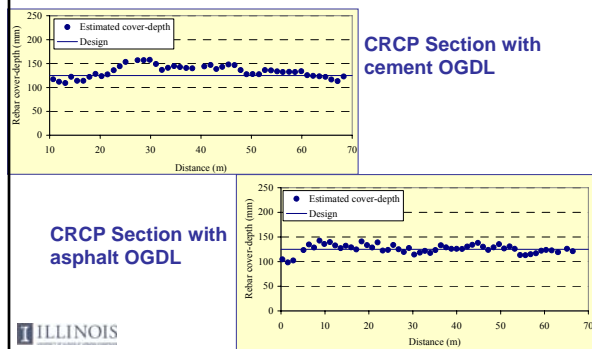
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Parabolic Shape Extraction from GPR



Rebar Cover-Depth Results



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Rebar Cover-Depth Accuracy

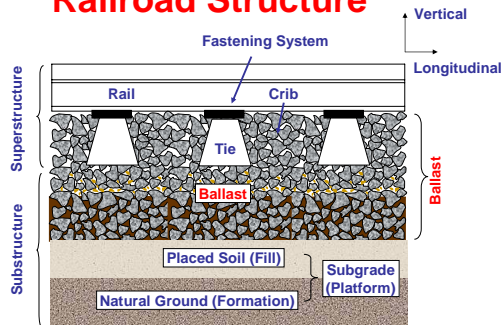
Comparison of GPR estimated cover-depth to CRCP cores from the VA Smart Road

	Core cover-depth (mm)	GPR cover-depth (mm)	Error (%)
Core 1	145	141	2.8
Core 2	121	118	2.5
Average error (%)			2.6

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Railroad Structure



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Clean and Fouled Ballast

Ballast fouling greatly influences its functions:

- **Clean ballast** : made of uniformly graded aggregates \Rightarrow large air voids.
- **Fouled ballast** : fouled by fine-grained material that fills air-voids.



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Dielectric Characteristics of Ballast

Dielectric constants of quartzite ballast

Railroad Ballast	Dielectric Constant
Dry, Clean Ballast	3.0
Wet, Clean Ballast (5% water)	3.5
Dry, Spent Ballast	4.3
Wet, Spent Ballast (5% water)	7.8
Saturated, Spent Ballast	38.5

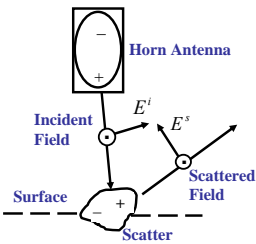
– Effect of moisture on fouled ballast is much greater than on clean ballast

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Scattering Analysis

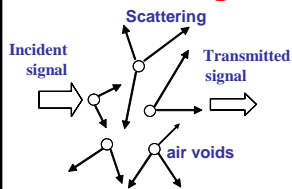
- Pavement Materials:
 - Scattering response is small
 - Reflected pulse has similar shape as incident signal
- Railroad Ballast:
 - Scattering response is dominant (heterogeneity is high)
 - Reflected pulse shape is influenced by scatter - air void



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EM Scattering from Air-Voids (cont.)



Attenuation Coefficient:

$$\alpha_s = \frac{N \cdot A}{2}$$

$$E = E_0 \cdot e^{-\alpha_s \cdot L}$$

N: number of particles per unit volume

Ballast degradation ⇒ Less air-voids ⇒ Less scattering ⇒ Less attenuation

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GPR Data Collection on Railroad



GPR Data Processing

Digital Signal Processing performed during data collection:

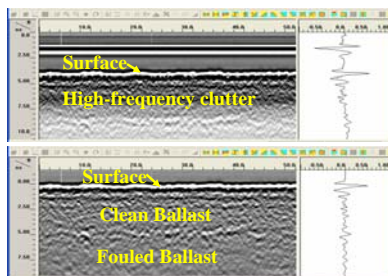
- Vertical band-pass FIR filter to remove noise
- Horizontal band-pass filter to remove clutter from rails
- Gain to account for energy attenuation



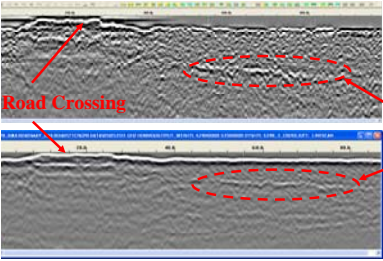
Processed GPR Data

First pulse from surface and subsequent small pulses are mainly from scattering

Raw GPR data



Trapped Water Detection



2 GHz

1 GHz

Road Crossing

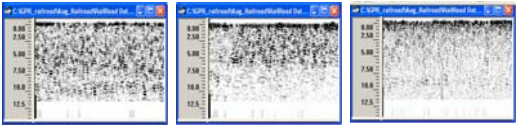
Trapped water due to lack of lateral drainage

2 GHz antenna is more sensitive to scattering pattern change than 1 GHz antenna.

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Scattering Analysis of Ballast under Different Conditions

GPR Data for different fouling conditions



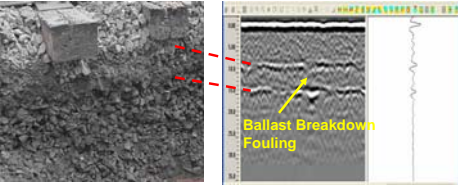
(a) Clean (b) Moderately fouled (c) Fouled

Ballast exhibiting various scattering patterns

Note: When ballast becomes fouled, interface between clean and fouled ballast is more difficult to find.

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Ballast Breakdown




Ballast Breakdown Fouling

Ballast breakdown under sleepers.

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Summary

- GPR is a NDE technique that can be used effectively to evaluate various transportation structures
- GPR can provide quick and reliable information about the subsurface.
- GPR reliable applications include:
 - Layer thickness estimation
 - Subsurface Moisture/ Distress detection
 - Rebar cover depth estimation
 - Rail Road evaluation (Ballast)
 - ...



Thank You!

Questions?